

**PILOT LEARNING
CALCULUS II ENGINEERING
PROBLEM-SET 2
FALL 2019**

(1) Evaluate the following integrals

(a)

$$\int \frac{dx}{\sin x}$$

(b)

$$\int \frac{dx}{x\sqrt{4x^2 + 1}}$$

(c)

$$\int \frac{dx}{x^3 + 1}$$

(d)

$$\int \frac{1 - x + 2x^2 - x^3}{x(x^2 + 1)^2} dx$$

(2) For which values of p does the integral

$$\int_0^{\infty} \frac{1}{x(\ln(x))^p} dx$$

converge?

(3) Let $A = \{(x, y) | x \geq 1, \frac{1}{x} \geq y \geq 0\}$. Is the area of A finite? What about the volume of the solid obtained by rotating A about the x axis?

(4) Match the following differential equations and possible solutions. (Note: The given functions may satisfy more than one equation or none, and some equations may have more than one solution.)

- | | |
|-----------------------|------------------------|
| a. $y'' = y$ | I. $y = \cos x$ |
| b. $y' = -y$ | II. $y = \cos(-x)$ |
| c. $y' = 1/y$ | III. $y = x^2$ |
| d. $y'' = -y$ | IV. $y = e^x + e^{-x}$ |
| e. $x^2 y'' - 2y = 0$ | V. $y = \sqrt{2x}$ |